

Arithmetical Progression

Is when a rank or Series of numbers differ orderly from one another, by some common number. To find the sum of any Arithmetical progression. add the first and last numbers together, and Multiply that sum by half the number of places and that product is the Sum. But if the number of places be odd multiply the Said number of places by half of the first and last added and the product is the Sum

1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16

What the sum

16	last
1	first
<hr/>	
17	sum
8	half the number of places
<hr/>	
136	Sum of the whole

Suppose a man hireth a room for a year, and agreeth to pay the first week 5 D, the second week 9 D, and so for the third week 13 D, so paying every week 4 D, more untill 52 weeks or a year is finished, Demand, what the rent will come to, — Answer 25. 3. 8

Here you are to consider that the common Increasing number is 4 D, so that the last week must amount to 51 times 4 added to the pay of the first week, which is 5 D, then will the last week come to 209 pence then work as in the Example,

D

$$\begin{array}{r} 51 \\ \frac{1}{4} \\ \text{Product } 20 \frac{1}{4} \\ \frac{5}{5} \\ \text{added } 209 \text{ the last week} \\ \frac{5}{5} \text{ the first week} \\ \text{added } 21 \frac{1}{4} \\ \frac{26}{26} \text{ half the weeks in a year} \\ \hline 128 \frac{1}{4} \\ \frac{428}{428} \\ \hline \text{Price } 556 \frac{1}{4} \end{array}$$

$$\begin{array}{r} 12 \overline{) 5564} \\ \underline{240} \\ 210 \overline{) 4638} \\ \underline{420} \\ 438 \\ \underline{438} \\ 0 \end{array}$$
 Answer

A man hired a horse for a year and was to pay for the first week 5s, and for the second week 9 farthings and the third 13s, and so on till the 52 weeks was finished what did the hire of this horse come to Demand

A man sold a house and giveth his Creditor a years time to pay for the said house (Viz) for the first week he was to pay 5s, the second week 9 farthings the third week 13s, so paying so more every week untill the 52 weeks was finished & what did that house Cost Demand

$$\begin{array}{r} 51 \\ \frac{1}{4} \\ \text{Product } 20 \frac{1}{4} \\ \frac{5}{5} \\ \text{added } 209 \text{ the last week} \\ \frac{5}{5} \text{ the first week} \\ \text{added } 21 \frac{1}{4} \\ \frac{26}{26} \text{ half the weeks in a year} \\ \hline 128 \frac{1}{4} \\ \frac{428}{428} \\ \hline 4 \overline{) 5564} \text{ Farthings} \\ \underline{128} \\ 128 \overline{) 1391 \frac{1}{4}} \\ \underline{210} \\ 210 \overline{) 11511} \\ \underline{515} \\ 515 \frac{1}{4} \text{ Answer} \end{array}$$

$$\begin{array}{r} 51 \\ \frac{1}{4} \text{ times } 51 \\ \text{Product } 20 \frac{1}{4} \\ \frac{5}{5} \\ \text{added } 209 \text{ the last week} \\ \frac{5}{5} \text{ the last week} \\ \text{added } 21 \frac{1}{4} \\ \frac{26}{26} \text{ half the weeks} \\ \hline 128 \frac{1}{4} \\ \frac{428}{428} \\ \hline 210 \overline{) 5564} \text{ Shillings } 86 \\ \underline{420} \\ 1364 \\ \underline{1364} \\ 0 \end{array}$$
 Answer

Supp 8 numbers wrought by the
Rule of Arithmetic progression
how many places Does it con-
tain Demand

$$\begin{array}{r}
 8 \text{ last number} \\
 1 \text{ first number} \\
 \hline
 9 \\
 4 \\
 \hline
 36 \text{ Answer in numbers}
 \end{array}$$

Which is equal to thus perform;

$$\begin{array}{r}
 1 \text{ number} \\
 2 \\
 3 \\
 4 \\
 5 \\
 6 \\
 7 \\
 8 \text{ last number} \\
 \hline
 36 \text{ Answer as before}
 \end{array}$$

Suppose you had a piece of Tobacco
Ground that lay three square
and the piece contained 60 rows
and the longest row 60 hills
deep and the shortest row 1 hill
how many hills is in that field
last Demand

$$\begin{array}{r}
 60 \\
 1 \text{ first number} \\
 \hline
 61 \\
 30 \text{ half the last number} \\
 \hline
 1830 \text{ Answer}
 \end{array}$$

Here I will say to make this
work show more plainly I
will suppose 6 rows of hills
and the longest to have 6 hills
and so every row to be one hill
shorter till it comes to one
how many hills is in that piece
of Ground Demand

$$\begin{array}{r}
 6 \text{ last row} \\
 1 \text{ hill the first} \\
 \hline
 7 \\
 3 \text{ half the last row} \\
 \hline
 21 \text{ number of hills}
 \end{array}$$

Or Thus performed



Facit 21 hills Thus

What the sum

$$\begin{array}{r}
 100 \text{ last} \\
 1 \text{ first number} \\
 \hline
 101 \\
 50 \text{ half the last num} \\
 \hline
 5050 \text{ Answer}
 \end{array}$$

What the Sum

As last
& first

$$\begin{array}{r}
 \text{Added } 45 \\
 \underline{22 \text{ half the last}} \\
 90 \\
 \underline{90} \\
 990 \text{ Answer}
 \end{array}$$

Equal to thus performed,

- 1
- 2
- 3
- 4
- 5
- 6
- 7
- 8
- 9
- 10
- 11
- 12
- 13
- 14
- 15
- 16
- 17
- 18
- 19
- 20
- 21
- 22
- 23
- 24
- 25
- 26
- 27
- 28
- 29
- 30
- 31
- 32
- 33
- 34
- 35
- 36
- 37
- 38
- 39
- 40
- 41
- 42
- 43
- 44

Added $\underline{990}$ Answer as before

Uneven numbers thus performed

$$\begin{array}{r}
 5 \\
 \underline{3} \\
 15
 \end{array}
 \left\{ \begin{array}{l}
 \text{Multiply the last num-} \\
 \text{ber by the last and} \\
 \text{first or the half of} \\
 \text{it but not add the} \\
 \text{first to the last only} \\
 \text{to make your Multi-} \\
 \text{plier}
 \end{array} \right.$$

Thus

What the sum

$$\begin{array}{r}
 15 \text{ last} \\
 \text{Multiplier } \underline{8} \\
 120 \text{ Facit}
 \end{array}
 \begin{array}{r}
 15 \\
 \underline{1} \text{ added} \\
 16 \\
 \underline{8 \text{ Multipli}}
 \end{array}$$

Or thus performed

- 1
- 2
- 3
- 4
- 5
- 6
- 7
- 8
- 9
- 10
- 11
- 12
- 13
- 14
- 15

$$\begin{array}{r}
 \underline{15} \\
 120 \text{ Answer as before } 86
 \end{array}$$

What the sum

$$\begin{array}{r}
 55 \text{ last} \\
 \underline{28 \text{ half the first \&}} \\
 440 \text{ and last} \\
 \underline{110 \text{ added}} \\
 1540 \text{ Answer}
 \end{array}$$

What the sum

7 last number
 1 first number and
 half the last &c

$$\text{Facit } \underline{\underline{28}}$$

Or thus Performed

1 first number
 2
 3
 4
 5
 6
 7 last number

$$\text{Facit } \underline{\underline{28}} \text{ as before \&c}$$

What the sum

5 last number
 3 Multiplier

$$\text{Facit } \underline{\underline{15}}$$

What the sum

9 last number
 5 Multiplier

$$\text{Facit } \underline{\underline{45}}$$

Or thus Proven &c



Facit 45 Thus

Count these Dots here above and they will show you the nature of the rule of Arithmetical progression all these Dots makes 45 hills of Tobacco of Taters or any kind of hills &c

What the sum last

95 last
 48 Multiplier

$$\begin{array}{r} 95 \text{ last} \\ 48 \text{ Multiplier} \\ \hline 760 \\ 380 \\ \hline \text{Facit } \underline{\underline{1140}} \end{array}$$

95 last
 1 first
 2 | 96 added
 48 Multiplier

Suppose you had a piece of Tobacco Ground that lay in a three square and the longest row contained 95 hills there every row one hill shorter till it come down to one hill how many hills does the 95 rows contain Demand

95 last number
 38 Multiplier

$$\begin{array}{r} 95 \text{ last number} \\ 38 \text{ Multiplier} \\ \hline 600 \\ 225 \\ \hline \text{Answer } \underline{\underline{2850}} \end{array}$$

What the sum the sum is 45 rows

hills 45 longest row
 23 Multiplier

$$\begin{array}{r} 45 \text{ longest row} \\ 23 \text{ Multiplier} \\ \hline 135 \\ 90 \\ \hline \text{Answer } \underline{\underline{1035}} \end{array}$$

Finis August 16th
 Day 1793

Geometrical Progression

Suppose one sold 12 Ells of Cloth to receive for the First ell 1D, the Second 2D, the third 4D, and so on Doubling what is paid for the 12 Ells?

0, 1, 2, 3, 4, 5, 6
1, 2, 4, 8, 16, 32, 64

Note. That if this Question had been for a Farthing a Button or the like, the Answer would have been farthings

32
108
192
2048
2
12 4096 Pence
2 0 34, 1 " 4
£17 " 1 " 4 Answer

Example

Suppose one sold a horse having 4 Shoes, and every Shoe 6 nails, to receive for the first nail 1 farthing the Second nail 2 farthings, the third nail a penny, and so Doubling, how much is paid for the last nail, and the price of the horse?

0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12,
1, 2, 4, 8, 16, 32, 64, 128, 256, 512, 1024, 2048, 4096.

8388608 farthings	2048
2	32768
Fact 16777216 farthings	16384
	81920
	Fact 8388608 far

Suppose a Man Sold a Coat that had on it 24 buttons
to receive for the first buttons 1 farthing the second 2 farthings
the third a penny and so Doubling till the 24 buttons was
finished what Did the Coat Cost Demand

0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12,
1, 2, 4, 8, 16, 32, 64, 128, 256, 512, 1024, 2048, 4096.

Suppose a Man Sold a Coat that
had on it 24 buttons to receive
for the first button 1 Grain of
Corn for the second 2 Grains and
for the third 4 Grains & so Dou-
bling till the 24 buttons were

	4096
	12288
	18432
	81920
	8388608
	2
41	16777216 farthings
12	4194304
20	3495215 1/2
	1747615 1/2 Answer

finished how much Corn did that Coat cost Allowing
400 Grains of Corn to the first Demand

0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12,
1, 2, 4, 8, 16, 32, 64, 128, 256, 512, 1024, 2048, 4096.

	Grains		4096
400	16777216	41943	Answer
	1600		12288
	777		18432
	400	in Pints	81920
	3772		8388608
	3600		2
	1724		16777216 Grains of Corn
	1600		
	1216		
	1200		

16/4/2 of a pint & C
400/100/50

Suppose Aman sold, that had on four shoes and each shoe had 6 Nails and to receive for the first nail 1 penny for the second 2 pence for the third Nail 4 pence &c. Doubling untill the 24 Nails were finished, what Did the last nail Come to, and the whole Amount of the horse Demand Thomas Perry August 19th Day 1793

- 0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12.
- 1, 2, 4, 8, 16, 32, 64, 128, 256, 512, 1024, 2048, 4096

4096 last Nail
 12288
 18432
 81920

 8388608
 2

12 16777216 Pence
 2p 13981014
6990511 in the Answer



o end Geometrical

Progression August
19th day 1793

Per Tom Perry