

Decimal Fractions

A decimal fraction is a fraction whose denominator is 1, with as many ciphers annexed as there are places in the numerator, and is usually expressed by writing the numerator only, with a point prefixed to it: thus $\frac{5}{10}$, $\frac{75}{100}$, $\frac{625}{1000}$ are decimal fractions, and are expressed by 5, .75, .625. — A mixed number consisting of a whole number and a decimal, as $25\frac{5}{10}$ is written thus 25.5. — as in numeration of whole numbers the values of the figures increase in a tenfold proportion from the right hand to the left; so in decimals, their values decrease in the same proportion, from the left hand to the right: which is exemplified in the following Table.

Hundred Million. Ten Million. Million. Hundred thousand. Ten thousand. Thousand. Hundred. Ten. Units.	Tenth. Hundredth. Thousandth. Ten thousandth. Hundred thousandth. Millionth. Ten Millionth. Hundred Millionth. Thousandth Millionth.
Whole Numbers.	Decimals.

Note. — Ciphers annexed to Decimals, neither increase nor decrease their value; thus 5, .50, .500, being $\frac{5}{10}$, $\frac{50}{100}$, $\frac{500}{1000}$, are of the same value: but ciphers prefixed to Decimals, decrease them in a tenfold proportion; thus 5, .05, .005, being $\frac{5}{10}$, $\frac{5}{100}$, $\frac{5}{1000}$, are of different values.

Addition of Decimals. Rule. place the given numbers according to their values; viz. units under units, tenths under tenths, &c. and add as in addition of whole numbers; observing to set the points in the sum exactly under those of the given numbers.

Examples.

.12	2.16	2.1
.134	8.45	4.12
.21	40.02	15.4
.743	35.4	76.26
.345	36.1	120.16
.002	125.32	425.04
<u>1.554</u> A	<u>242.45</u> A	<u>643.58</u> Ans

Add 5, 123, 75, 496 and 750 together.

Subtraction of Decimals.

Rule. — place the numbers as in addition, with the less under the greater, and subtract as in whole numbers; setting the point in the remainder under those in the given numbers. —

Examples.

.4562	56.12	.4314
.316	1.242	.312
<u>1402</u>	<u>54.878</u>	<u>1.194</u>

From 100.14 take 1.146

100.14	1.146
<u>99.024</u>	Answers

Multiplication of Decimals.

Rule. — Multiply as in whole numbers, and point off in the product as many Decimal places as there are in both factors.

If there are not as many places in the product as there are Decimals places in the factors, prefix

Ciphers to supply the deficiency

Examples.

1. Multiply .612 by 4.12

.612	4.12
2448	
612	
<u>252144</u>	Answer

2. Multiply 1.007 by .041

1.007	.041
4028	
<u>.041287</u>	Answer

3. Multiply 37.9 by 46.5

37.9	46.5
1895	
2274	
<u>176235</u>	Answer

Division of Decimals.

Rule. — Divide as in whole numbers, and from the right hand of the quotient point off as many places for Decimals as the decimal places in the dividend exceed those in the Divisor.

If the places of the quotient are not so many as the rule requires, supply the defect by prefixing Ciphers. If at any time there be a remainder, or the decimal places in the divisor be more than those in the dividend, Ciphers may be affixed to the Dividend, and the quotient carried on to any Degree of exactness.

Examples.

Divide .863972 by 92.

$$\begin{array}{r}
 92 \overline{) .863972} \quad (.009394 \text{ Answer}) \\
 \underline{828} \\
 359 \\
 \underline{276} \\
 837 \\
 \underline{828} \\
 92 \\
 \underline{92} \\
 0
 \end{array}$$

Divide 4.13 by 572.4

$$\begin{array}{r}
 572.4 \overline{) 4.130000} \quad (.00721 \text{ Answer}) \\
 \underline{40068} \\
 12320 \\
 \underline{11448} \\
 8720 \\
 \underline{5724} \\
 2996
 \end{array}$$

Divide 19.25 by 38.5

$$\begin{array}{r}
 38.5 \overline{) 19.25} \quad (.5 \text{ Answer}) \\
 \underline{1925} \\
 \dots
 \end{array}$$

Divide .1606 by .44

$$\begin{array}{r}
 .44 \overline{) .1606} \quad (.365 \text{ Answer}) \\
 \underline{132} \\
 286 \\
 \underline{264} \\
 220 \\
 \underline{220} \\
 \dots
 \end{array}$$

Divide .1606 By 4.4

$$\begin{array}{r}
 4.4 \overline{) .1606} \quad (.0365 \text{ Answer}) \\
 \underline{132} \\
 286 \\
 \underline{264} \\
 220 \\
 \underline{220} \\
 \dots
 \end{array}$$

Divide .1606 By 44.

$$\begin{array}{r}
 44 \overline{) .1606} \quad (.00365 \text{ Answer}) \\
 \underline{132} \\
 286 \\
 \underline{264} \\
 220 \\
 \underline{220} \\
 \dots
 \end{array}$$

Divide 9. by 9 Result 10.

$$\begin{array}{r}
 9 \overline{) 9} \quad (10 \text{ Answer}) \\
 \underline{9} \\
 \dots
 \end{array}$$

Divide 9 by 9. Result 1

$$\begin{array}{r}
 9 \overline{) 9} \quad (1 \text{ Answer}) \\
 \underline{9} \\
 \dots
 \end{array}$$

Divide 186.9 By 7.476 An. 25.

$$\begin{array}{r}
 7.476 \overline{) 18690} \quad (25 \text{ Answer}) \\
 \underline{14952} \\
 37380 \\
 \underline{37380} \\
 \dots
 \end{array}$$

72.4103 2508.928065051 (27.1498

$$\begin{array}{r}
 72.4103 \overline{) 2508.928065051} \quad (27.1498 \text{ Answer}) \\
 \underline{18482070} \\
 66072106 \\
 \underline{64687245} \\
 13848615 \\
 \underline{9241035} \\
 46075800 \\
 \underline{36064140} \\
 91116605 \\
 \underline{83169315} \\
 77472701 \\
 \underline{73928280} \\
 5544621
 \end{array}$$

Reduction of Decimals.

Case 1. To reduce a vulgar fraction to a Decimal. Rule. annex as many ciphers to the numerator as may be necessary, and divide it by the denominator.

Note. - There must be as many Decimal places in the quotient as there are ciphers annexed to the numerator. When compound fractions is given, first reduce it to a single one, and then to a decimal.

Examples.

Reduce $\frac{1}{4}$ to a decimal fraction

$$\begin{array}{r} 4 \overline{) 1.00} \\ \underline{.25} \end{array} \text{ Answer}$$

Reduce $\frac{1}{2}$ to a Decimal

$$\begin{array}{r} 2 \overline{) 1.0} \\ \underline{.5} \end{array} \text{ Answer}$$

Reduce $\frac{3}{4}$ to a Decimal

$$\begin{array}{r} 4 \overline{) 3.00} \\ \underline{.75} \end{array}$$

Reduce $\frac{3}{8}$ to a Decimal

$$\begin{array}{r} 8 \overline{) 3.000} \\ \underline{.375} \end{array} \text{ Answer}$$

Case 2. To reduce any sum or quantity, to the decimal of any given denomination.

Rule. - Divide the given sum or quantity reduced to the lowest denomination mentioned, by the proposed Integer, reduced to the same denomination, and the quotient will be the decimal required.

Examples.

Reduce 17 6 to the decimal of a Pound

$$\begin{array}{r} \text{S. D.} \\ 20 \overline{) 176} \\ \underline{240} \\ 240 \overline{) 210.000} \\ \underline{1920} \\ 1800 \\ \underline{1680} \\ 1200 \\ \underline{1200} \end{array} \text{ Answer } .875$$

Reduce 7 6 to the decimal of a £.

$$\begin{array}{r} \text{S. D.} \\ 12 \overline{) 76} \\ 240 \overline{) 90.000} \\ \underline{720} \\ 1800 \\ \underline{1680} \\ 1200 \\ \underline{1200} \end{array} \text{ Answer } .375$$

Reduce 9 to the decimal of a £.

$$\begin{array}{r} 240 \overline{) 20000} \\ \underline{720} \\ 1800 \\ \underline{1680} \\ 1200 \\ \underline{1200} \end{array} \text{ Answer } .0375$$

Reduce 3 qrs 2 s. to the Decimal

$$\begin{array}{r} 16 \overline{) 14000} \\ \underline{1280} \\ 120 \\ \underline{112} \\ 80 \\ \underline{80} \end{array} \text{ Answer } .875$$

Reduce 1 pint to the Denominator of a Gallon.

$$\begin{array}{r} \text{Pint } 8 \text{ } \underline{1.000} \\ .125 \text{ Answer} \end{array}$$

CASE 3. — To reduce a decimal fraction to its value.

Rule. Multiply it by the known parts of the Integer, and separate to the right of the product as many places as there are places in the given number.

Examples.

What is the value of .875 of a £

$$\begin{array}{r} .875 \\ \underline{20} \\ 17.500 \\ \underline{12} \\ 6.000 \end{array}$$

$$\begin{array}{r} \text{£ } 17 \text{ } 6 \text{ Answer} \end{array}$$

What is the value of .87615 of a pound? — — —

$$\begin{array}{r} .87615 \\ \underline{20} \\ 17.52300 \\ \underline{12} \\ 6.27600 \\ \underline{4} \\ 1.10400 \end{array}$$

$$\begin{array}{r} \text{£ } 17 \text{ } 6 \frac{1}{4} \text{ Answer} \end{array}$$

What is the value of .7854166 of a Pound? — — —

$$\begin{array}{r} .7854166 \\ \underline{20} \\ 15.7083320 \\ \underline{12} \\ 8.4999840 \\ \underline{4} \\ 1.9999360 \end{array}$$

$$\begin{array}{r} \text{£ } 15 \text{ } 8 \frac{1}{4} \text{ Answer} \end{array}$$

What is the value of $\frac{76}{100}$ of a Pound

$$\begin{array}{r} .76 \\ \underline{20} \\ 15.20 \\ \underline{12} \\ 2.40 \\ \underline{4} \end{array}$$

$$\begin{array}{r} \text{£ } 15 \text{ } 2 \frac{1}{4} \text{ Answer} \end{array}$$

What is the value of .625 of a Shilling

$$\begin{array}{r} .625 \\ \underline{12} \\ 7.500 \\ \underline{4} \end{array}$$

$$\begin{array}{r} \text{D } 7 \frac{1}{2} \text{ Answer} \end{array}$$

What is the value of .461 of a Dollar?

$$\begin{array}{r} .461 \\ \underline{100} \\ 46.100 \\ \underline{10} \\ 1.000 \end{array}$$

$$\begin{array}{r} \text{Cent } 46 \text{ } 1 \text{ Answer} \end{array}$$

What is the value of .86 of a bush?

$$\begin{array}{r}
 .86 \\
 \underline{4} \\
 3.44 \\
 \underline{28} \\
 12.32 \\
 \underline{16} \\
 5.12 \\
 \underline{16} \\
 1.92
 \end{array}$$

2 16 05 27.
 3 12 5 1.92 Answer

What is the value of .7 of a lb.
 Troy? Demand

$$\begin{array}{r}
 .7 \\
 \underline{12 \text{ ounces 1 pound Troy}} \\
 8.4 \\
 \underline{20} \\
 8.0 \\
 \text{oz. Part} \\
 8 \quad 8 \text{ Answer}
 \end{array}$$

What is the value of .71 of 4^{oz.}
 Troy? Demand

$$\begin{array}{r}
 .71 \\
 \underline{4 \text{ oz.}} \\
 2.84 \\
 \underline{20} \\
 16.80 \\
 \underline{28} \\
 19.20
 \end{array}$$

oz. Part 9⁴
 2 16 19 20 Answer

What is the .761 of a Day
 Decimally Expressed

$$\begin{array}{r}
 .761 \\
 \underline{24} \\
 3044 \\
 \underline{1522} \\
 18.264 \\
 \underline{60} \\
 15.840
 \end{array}$$

4 the Seconds
 18 15 50 400

Answer

What is the .67 of a League
 Decimally Expressed

$$\begin{array}{r}
 .67 \\
 \underline{3 \text{ Miles}} \\
 2.01 \\
 \underline{8 \text{ Furlongs}} \\
 .08 \\
 \underline{40} \\
 3.20 \\
 \underline{18 \text{ half yards}} \\
 25220 \\
 \underline{110 \text{ yards}} \\
 3 \\
 .30
 \end{array}$$

11 fur Poles yd
 2 0 3 1 .30 Answer

What is the value of .712 of a
 Furlong? Demand

$$\begin{array}{r}
 .712 \\
 \underline{40 \text{ Poles}} \\
 28.480 \\
 \underline{11} \\
 255280 \\
 \underline{2640 \text{ yards}} \\
 3 \\
 1.920 \text{ feet} \\
 \underline{12} \\
 11040 \text{ Inches}
 \end{array}$$

Poles yd ft in
 28 2 1 11 .040 Answer

What is the value of .6875 of
 a yard? Demand

$$\begin{array}{r}
 .6875 \\
 \underline{4} \\
 27500 \\
 \underline{4} \\
 30000
 \end{array}$$

27 3 3 Answer

What is the value of .3375 of a
Cwt? Demand

$$\begin{array}{r} .3375 \\ \underline{4} \\ 13500 \\ \underline{40} \\ 140000 \end{array}$$

Ans. Pwt
1 14 Answer

What is the value of .3 of an
year? Demand

$$\begin{array}{r} .3 \\ \underline{365} \\ 1095 \\ \underline{24} \\ 120 \end{array}$$

Days $\frac{1}{2}$
109 12 Answer

What is the value of .07 of a
Barrel of 22 Gallons?

$$\begin{array}{r} .07 \\ \underline{32} \\ 214 \\ \underline{21} \\ 224 \\ \underline{8} \\ 192 \end{array}$$

Gal. Pint
2 1 92 Answer

What is the value of 48 of a
Pound, and the .16 of a Shilling

$$\begin{array}{r} .48 \\ \underline{20} \\ 960 \\ \underline{12} \\ 920 \end{array} \quad \begin{array}{r} .16 \\ \underline{12} \\ 192 \end{array}$$

$\frac{1}{2}$ D
9 7 92
1 20
9 9 12 Answer

What is the sum of .17 of a Pound
Troy and .84 of an Ounce?

$$\begin{array}{r} .17 \\ \underline{12} \\ 204 \\ \underline{20} \\ 80 \\ \underline{24} \\ 1920 \end{array} \quad \begin{array}{r} .84 \\ \underline{20} \\ 1680 \\ \underline{24} \\ 1920 \end{array}$$

$\frac{1}{2}$ P. Oz.
2 0 19 20
16 19 20
2 17 14 40 Answer

What is the Difference between
.17 Pound $\frac{1}{2}$? Demand

$$\begin{array}{r} .17 \\ \underline{20} \\ 340 \\ \underline{12} \\ 480 \\ \underline{4} \\ 820 \end{array} \quad \begin{array}{r} \frac{1}{2} \\ \underline{12} \\ 84 \\ \underline{4} \\ 16 \end{array}$$

$\frac{1}{2}$ D
3 4 3/4 20
8 1/4 .6
2 8 1/2 14 Answer

What is the Difference between
.41 Day and .16 Hour?

$$\begin{array}{r} .41 \\ \underline{24} \\ 164 \\ \underline{82} \\ 984 \\ \underline{60} \\ 5040 \\ \underline{60} \\ 2400 \end{array} \quad \begin{array}{r} .16 \\ \underline{60} \\ 960 \\ \underline{60} \\ 3600 \end{array}$$

Days $\frac{1}{2}$ Seconds
9 50 24
0 9 36
9 40 48 Answer